



Cambridge International A Level

MATHEMATICS

9709/52

Paper 5 Probability & Statistics 1

October/November 2020

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2020 series for most Cambridge IGCSE™, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

This document consists of **14** printed pages.

PUBLISHED**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mathematics Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

PUBLISHED**Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

DM or DB When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

PUBLISHED**Abbreviations**

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1(a)	$1 - \left(\frac{5}{6}\right)^5$ or $\frac{1}{6} + \frac{5}{6} \times \frac{1}{6} + \left(\frac{5}{6}\right)^2 \times \frac{1}{6} + \left(\frac{5}{6}\right)^3 \times \frac{1}{6} + \left(\frac{5}{6}\right)^4 \times \frac{1}{6}$	M1	$1 - p^n$ $n = 5, 6$ or $p + pq + pq^2 + pq^3 + pq^4 (+ pq^5)$ $0 < p < 1, p + q = 1,$
	$0.598, \frac{4651}{7776}$	A1	
		2	
1(b)	$(1 - P(0, 1, 2))$ $1 - \left(\left(\frac{5}{6}\right)^{10} + {}^{10}C_1 \left(\frac{1}{6}\right) \left(\frac{5}{6}\right)^9 + {}^{10}C_2 \left(\frac{1}{6}\right)^2 \left(\frac{5}{6}\right)^8 \right)$	M1	${}^{10}C_x p^x (1-p)^{10-x}, 0 < p < 1, \text{ any } p, x \neq 0, 10$
	$1 - (0.1615056 + 0.3230111 + 0.290710)$	A1	Correct expression, accept unsimplified, condone omission of final bracket
	0.225	A1	$0.2247 < p \leq 0.225, \text{ WWW}$
		3	

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Question	Answer	Marks	Guidance															
2(a)	$P(1 \text{ red}) = \frac{5}{8} \times \frac{3}{7} \times \frac{2}{6} \times 3$	M1	$\frac{a}{8} \times \frac{b}{7} \times \frac{c}{6} \times k$ or $\frac{5}{d} \times \frac{3}{e} \times \frac{2}{f} \times 3, 1 \leq a, b, c \leq 5, d, e, f \leq 8, a, b, c, d, e, f, k$ all integers. $1 < k \leq 3,$															
	$\frac{15}{56}$	A1	AG, WWW															
Alternative method for question 2(a)																		
	$\frac{{}^5C_1 \times {}^3C_2}{{}^8C_3}$	M1	$\frac{{}^aC_1 \times {}^bC_2}{{}^8C_3}$ or $\frac{{}^5C_d \times {}^3C_e}{{}^8C_3}$ or $\frac{{}^5C_d \times {}^3C_e (or {}^aC_1 \times {}^bC_2)}{{}^5C_3 \times {}^3C_0 + {}^5C_2 \times {}^3C_1 + {}^5C_1 \times {}^3C_2 + {}^5C_0 \times {}^3C_3}, a + b = 8, d + e = 3$															
	$\frac{15}{56}$	A1	AG, WWW, $\frac{15}{56}$ must be seen															
		2																
2(b)	<table border="1" data-bbox="322 975 898 1217"> <tr> <td>x</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> </tr> <tr> <td>Prob.</td> <td>$\frac{1}{56}$</td> <td>$\frac{15}{56}$</td> <td>$\frac{30}{56} = \frac{15}{28}$</td> <td>$\frac{10}{56} = \frac{5}{28}$</td> </tr> <tr> <td></td> <td>0.0179</td> <td>0.268</td> <td>0.536</td> <td>0.179</td> </tr> </table>	x	0	1	2	3	Prob.	$\frac{1}{56}$	$\frac{15}{56}$	$\frac{30}{56} = \frac{15}{28}$	$\frac{10}{56} = \frac{5}{28}$		0.0179	0.268	0.536	0.179	B1	Probability distribution table with correct outcomes with at least one probability less than 1, allow extra outcome values if probability of zero stated. B1 2 of P(0), P(2) and P(3) correct B1 FT 4 th probability correct or FT sum of 3 or more probabilities = 1, with P(1) correct 3
x	0	1	2	3														
Prob.	$\frac{1}{56}$	$\frac{15}{56}$	$\frac{30}{56} = \frac{15}{28}$	$\frac{10}{56} = \frac{5}{28}$														
	0.0179	0.268	0.536	0.179														

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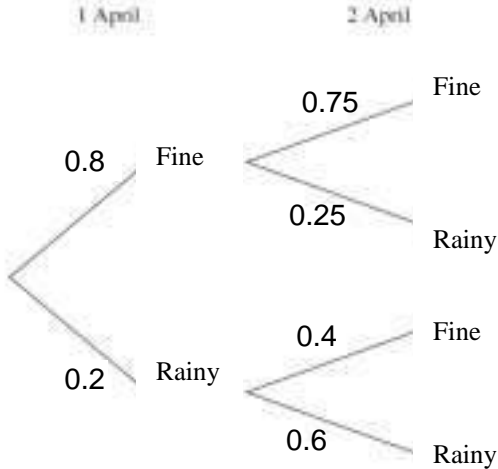
Question	Answer	Marks	Guidance
2(c)	$\text{Var}(X) = \frac{(0^2 \times 1) + 1^2 \times 15 + 2^2 \times 30 + 3^2 \times 10}{56} - \left(\frac{15}{8}\right)^2$ $= \frac{15}{56} + \frac{120}{56} + \frac{90}{56} - \left(\frac{15}{8}\right)^2$	M1	Substitute <i>their</i> attempts at scores in correct variance formula, must have ‘– mean ² ’ (FT if mean calculated) (condone probabilities not summing to 1 for this mark)
	$\frac{225}{448}, 0.502$	A1	
		2	

Question	Answer	Marks	Guidance
3(a)	$P(X > 11.3) = P\left(z > \frac{11.3 - 10.1}{1.3}\right) = P(z > 0.9231)$	M1	Using \pm standardisation formula, no $\sqrt{\sigma}$ or σ^2 , continuity correction
	$1 - 0.822$	M1	Appropriate area Φ , from standardisation formula $P(z > \dots)$ in final solution
	0.178	A1	0.1779...
		3	
3(b)	$z = -0.674$	B1	± 0.674 seen (critical value)
	$\frac{t - 10.1}{1.3} = -0.674$	M1	An equation using \pm standardisation formula with a z -value, condone $\sqrt{\sigma}$ or σ^2 , continuity correction.
	$t = 9.22$	A1	AWRT. Only dependent on M1
		3	

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Question	Answer	Marks	Guidance
3(c)	$P(8.9 < X < 11.3) = 1 - 2 \times \text{their 3(a)}$ $\equiv 2(1 - \text{their 3(a)}) - 1$ $\equiv 2(0.5 - \text{their 3(a)})$ $= 0.644$	B1 FT	FT from <i>their 3(a)</i> < 0.5 or correct, accept unevaluated probability OE
	Number of days = 90×0.644 = 57.96	M1	$90 \times \text{their } p$ seen, $0 < p < 1$
	So 57 (days)	A1 FT	Accept 57 or 58, not 57.0 or 58.0, no approximation/rounding stated FT must be an integer value
	Alternative method for question 3(c)		
	$P\left(\frac{8.9 - 10.1}{1.3} < z < \frac{11.3 - 10.1}{1.3}\right)$ $= \Phi(0.9231) - (1 - \Phi(0.9231))$ oe $= 0.822 - (1 - 0.822)$ $= 0.644$	B1	Accept unevaluated probability
	Number of days = 90×0.644 = 57.96	M1	$90 \times \text{their } p$ seen, $0 < p < 1$
	So 57 (days)	A1 FT	Accept 57 or 58, not 57.0 or 58.0, no approximation/rounding stated FT must be an integer value
	3		

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Question	Answer	Marks	Guidance
4(a)		B1	All probabilities correct, may be on branch or next to 'Fine/Rainy' Ignore additional branches.
		1	
4(b)	$0.8 \times 0.75 + 0.2 \times 0.4$ (= 0.6 + 0.08)	M1	Correct or FT from <i>their</i> diagram unsimplified, all probabilities $0 < p < 1$. Partial evaluation only sufficient when correct. Accept working in 4(b) or by the tree diagram.
	$0.68, \frac{17}{25}$	A1	From supporting working
		2	

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Question	Answer	Marks	Guidance
4(c)	$0.8 \times 0.75 \times 0.25 + 0.8 \times 0.25 \times 0.6$	M1	$a \times b \times c + a \times 1-b \times d, 0 < c, d \leq 1,$ a, b consistent with <i>their</i> tree diagram or correct, no additional terms
	0.15 + 0.12	A1	At least one term correct, accept unsimplified
	0.27	A1	Final answer
		3	
4(d)	$P(Y) = \textit{their} (c) + 0.2 \times 0.4 \times 0.25 + 0.2 \times 0.6 \times 0.6$ (= 0.362)	B1 FT	$\textit{their} (c) + e \times f \times g + e \times (1-f) \times h, 0 < g, h \leq 1, e, f$ consistent with <i>their</i> tree diagram, or correct
	$P(X Y) = \frac{\textit{their} (c)}{\textit{their} P(Y)} = \frac{0.27}{0.362}$	M1	$\textit{their} 4(c)$ (or correct)/ \textit{their} previously calculated and identified $P(Y)$ or a denominator involving 3 or 4 3-factor probability terms consistent with <i>their</i> tree diagram & third factor $0 < p < 1$
	$0.746, \frac{373}{500}$ or $\frac{135}{181}$	A1	(0.7458...)
		3	

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Question	Answer	Marks	Guidance																		
5(a)	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; border-bottom: 1px solid black; text-align: center;"><i>Dados</i></td> <td style="width: 5%;"></td> <td style="width: 45%; border-bottom: 1px solid black; text-align: center;"><i>Linva</i></td> </tr> <tr> <td style="text-align: center;">8 6 0</td> <td style="text-align: center;"> </td> <td style="text-align: center;">0 2 9</td> </tr> <tr> <td style="text-align: center;">6 5 2 0 0</td> <td style="text-align: center;"> </td> <td style="text-align: center;">0 1 2 5 6</td> </tr> <tr> <td style="text-align: center;">8 2 2</td> <td style="text-align: center;"> </td> <td></td> </tr> <tr> <td style="text-align: center;">6 3 2 6</td> <td style="text-align: center;"> </td> <td></td> </tr> <tr> <td style="text-align: center;">2 4 0</td> <td style="text-align: center;"> </td> <td></td> </tr> </table>	<i>Dados</i>		<i>Linva</i>	8 6 0		0 2 9	6 5 2 0 0		0 1 2 5 6	8 2 2			6 3 2 6			2 4 0			B1	Correct stem can be upside down, ignore extra values
	<i>Dados</i>		<i>Linva</i>																		
	8 6 0		0 2 9																		
	6 5 2 0 0		0 1 2 5 6																		
	8 2 2																				
6 3 2 6																					
2 4 0																					
		B1	Correct Dados labelled, leaves in order and lined up vertically (less than midway to next column), no commas etc, no extra terms																		
		B1	Correct Linva on opposite side of stem labelled, leaves in order and lined up vertically (less than midway to next column), no commas etc, no extra terms																		
		B1	Correct single key for their diagram, need both resorts identified and 'cm' stated at least once here or in leaf headings or title. SC If 2 separate diagrams drawn, SCB1 if both keys meet these criteria B0B1B0SCB1 max.																		
	KEY 6 3 2 means 36 cm (snow) in Dados and 32 cm (snow) in Linva	4																			
5(b)	Median or Q2 = 15 (cm)	B1	Correct																		
	UQ or Q3 = 28 cm, LQ or Q1 = 10 cm IQR = 28 – 10	M1	$22 \leq UQ \leq 36 - 8 \leq LQ \leq 10$																		
	18 (cm)	A1	WWW																		
		3																			
5(c)	On average the snowfall in Davos is higher	B1 FT	FT from <i>their</i> 5(b) values for Dados. Statement comparing central tendency in context																		
	The amount of snowfall in Linva varies more than in Davos	B1 FT	Statement comparing spread in context Note: simply stating and comparing the values is not sufficient.																		
		2																			

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Question	Answer	Marks	Guidance	
6(a)	${}^9C_6 (\times {}^3C_3)$	M1	${}^9C_k \times n, k = 6, 3, n = 1, 2$ oe Condone ${}^9C_6 + {}^3C_3, {}^9P_6 \times {}^3P_3$	
	84	A1	Accept unevaluated.	
		2		
6(b)	Number with 3 Baker children = 6C_2 or 15	B1	Correct seen anywhere, not multiplied or added	
	Total no of selections = 9C_5 or 126 Probability = $\frac{\text{number of selections with 3 Baker children}}{\text{total number of selections}}$	M1	Seen as denominator of fraction	
	$\frac{15}{126}, 0.119$	A1	OE, e.g. $\frac{5}{42}$	
	Alternative method for question 6(b)			
	$\frac{3}{9} \times \frac{2}{8} \times \frac{1}{7} \left(\times \frac{6}{6} \right) \left(\times \frac{5}{5} \right) \times {}^5C_3$	B1	5C_3 (OE) or 10 seen anywhere, multiplied by fractions only, not added	
		M1	$\frac{3}{9} \times \frac{2}{8} \times \frac{1}{7} \left(\times \frac{6}{6} \right) \left(\times \frac{5}{5} \right) \times k, 1 \leq k, k \text{ integer}$	
	$\frac{15}{126}, 0.119$	A1	OE, e.g. $\frac{5}{42}$	
	3			

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Question	Answer	Marks	Guidance
6(c)	[Total no of arrangements = 9!] [Arrangements with men together = $8! \times 2$]	M1	$9! - k$ or $362880 - k$, k an integer < 362 880
	Not together: $9! -$		
	$8! \times 2$	B1	$8! \times 2(!)$ or 80 640 seen anywhere
	282 240	A1	Exact value
	Alternative method for question 6(c)		
	$7! \times 8 \times 7$	B1	$7! \times k$, k positive integer > 1
		M1	$m \times 8 \times 7$, $m \times {}^8P_2$, $m \times {}^8C_2$, m positive integer > 1
	282 240	A1	Exact value
	3		
6(d)	$7! \times 2 \times 7$	M1	$7! \times k$, k positive integer > 1 If 7! not seen, condone $7 \times 6 \times 5 \times 4 \times 3 \times 2 \times (1) \times k$ or $7 \times 6! \times k$ only
		M1	$m \times 2 \times 7$, m positive integer > 1
	70 560	A1	
		3	